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# Crystal Structures and Solid-State Photochemistry of Dimorphic Dibenzobarrelenes: Enantioselectivity of the Di- $\pi$-methane Rearrangement in the Solid State 

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#### Abstract

The diisopropyl diester derivative of dibenzobarrelene is dimorphic; one of the dimorphs crystallizes in a chiral space group ( $P 2_{1} 2_{1} 2_{1}$ ), while the other crystallizes in an achiral space group ( $P b c a$ ). The chiral crystal undergoes a stereospecific photorearrangement to yield the corresponding dibenzosemibullvalene in near-quantitative enantiomeric excess, and the absolute configurations of the starting material and the product have been determined (with reasonable, although not complete certainty). Steric arguments, coupled with the absolute configurational relationship between the starting material and its photoproduct, have been used to rationalize the enantioselective pathway of the rearrangement in the solid state. Crystal data are: $T=295 \mathrm{~K}, \mathrm{Mo} K \alpha_{1}$, $\lambda=0.70930 \AA, \quad$ or $\mathrm{Cu} K \alpha_{1}, \quad \lambda=1.54056 \AA$; diisopropyl 9,10-dihydro-9, 10 -ethenoanthracene-11,12dicarboxylate (form $a,{ }^{i} \operatorname{Pr} / i \operatorname{Pr}-a$ ), $\mathrm{C}_{24} \mathrm{H}_{24} \mathrm{O}_{4}, M_{r}=$ 376.45, orthorhombic, $P 2_{1} 2_{2} 2_{1}, a=8 \cdot 3488$ (9), $b=$ 11.7036 (9), $c=21.8060$ (13) $\AA, V=2130.7$ (3) $\AA^{3}, Z$ $=4, D_{x}=1.173 \mathrm{~g} \mathrm{~cm}^{-3}, \mu(\mathrm{Cu})=6.0 \mathrm{~cm}^{-1}, F(000)$ $=800, R=0.069$ for 3101 observed reflections; diisopropyl 9,10-dihydro-9,10-ethenoanthracene-11,12dicarboxylate (form $b,{ }^{i} \operatorname{Pr} /{ }^{i} \mathrm{Pr}-b$ ), $\mathrm{C}_{24} \mathrm{H}_{24} \mathrm{O}_{4}, M_{r}=$ 376.45, orthorhombic, Pbca, $a=9.738$ (2), $b=$ 17.092 (3), $c=25.080$ (5) $\AA, V=4174$ (1) $\AA^{3}, Z=8$, $D_{x}=1.198 \mathrm{~g} \mathrm{~cm}^{-3}, \quad \mu(\mathrm{Mo})=0.75 \mathrm{~cm}^{-1}, \quad F(000)=$


$1600, R=0.044$ for 1299 observed reflections; diisopropyl $4 \mathrm{~b}, 8 \mathrm{~b}, 8 \mathrm{c}, 8 \mathrm{~d}-$ tetrahydrodibenzo $[a, f]$ cyclo-propa[cd]pentalene-8c, 8 d -dicarboxylate ( ${ }^{( } \mathrm{Pr} /{ }^{\mathrm{i}} \mathrm{Pr}-a p$ ), $\mathrm{C}_{24} \mathrm{H}_{24} \mathrm{O}_{4}, \quad M_{r}=376 \cdot 45$, tetragonal, $P 4_{3} 2_{2} 2, a=$ $10 \cdot 1889$ (2), $c=38.6347$ (5) $\AA, V=4010 \cdot 8(1) \AA^{3}, Z$ $=8, D_{x}=1.247 \mathrm{~g} \mathrm{~cm}^{-3}, \mu(\mathrm{Cu})=6.4 \mathrm{~cm}^{-1}, \quad F(000)$ $=1600, R=0.036$ for 2879 observed reflections. The molecular structures of the dimorphs are similar to each other, except in the region of the $\alpha, \beta$-unsaturated carbonyl system where the extents of conjugation of the ester groups to the central double bond are different in the two dimorphs. The ring skeletons of the dibenzobarrelenes and the dibenzosemibullvalene are similar to the corresponding units of the unsymmetrical 11,12-diester derivatives in previous work. The enantioselective pathway leading to the formation of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$ is consistent with steric packing effects, estimated from qualitative visual inspection of the packing environment around the ester groups, and from van der Waals intermolecular steric energy changes resulting from the movement of the ester groups.

## Introduction

Previous crystal structure studies of 11,12-diester derivatives of dibenzobarrelene with non-equivalent ester groups ( $E^{\prime} \neq E$, Fig. 1) (Garcia-Garibay,

[^0]Scheffer, Trotter \& Wireko, 1990; Garcia-Garibay, 1988; Scheffer, Trotter, Garcia-Garibay \& Wireko, 1988) have given detailed information on the structural aspects of the regioselective pathways in the solid-state photochemistry of this class of compound. These reactions proceed via the di- $\pi$-methane rearrangement (Zimmerman, 1980; Hixson, Mariano \& Zimmerman, 1973; Zimmerman, Keck \& Pflederer, 1976) to give, in general, two photoproducts (2) and (2'), which are regioisomerically related (Fig. 1), together with their enantiomorphs. The pathways leading to the formation of the major products in the solid state have been examined from electronic and steric points of view; correlation of structural and photochemical data has shown that the favoured pathways are explicable in terms of steric packing factors (Garcia-Garibay et al., 1990).
In the present paper we report that the diisopropyl diester derivative of dibenzobarrelene ( $E^{\prime}=E=$ $\mathrm{CO}_{2}{ }^{i} \mathrm{Pr}$ ) is dimorphic. The molecule is achiral, but the dimorph designated ${ }^{\circ} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ crystallizes in a chiral space group ( $P 2_{1} 2_{1} 2_{1}$ ). Photolysis of the crystals of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ shows the production of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$ in quantitative enantiomeric excess (Evans, GarciaGaribay, Omkaram, Scheffer, Trotter \& Wireko, 1986); similar treatment of the other dimorph, designated ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-b$ (achiral space group Pbca), gives no optically active photoproducts. The electronic and steric arguments that were employed in an attempt to explain the regioselectivity in the solid state of the unsymmetrical 11,12-diester derivatives (GarciaGaribay et al., 1990) are invoked in order to rationalize the observed enantioselectivity of the photochemical rearrangement of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ in the solid state.


Fig. 1. Di - $\pi$-methane rearrangement in dibenzobarrelenes $(E=$ $\mathrm{CO}_{2} R$ ).

## Experimental

It was observed during preliminary X-ray crystallographic investigation of the crystals of the diisopropyl diester derivative of dibenzobarrelene grown from cyclohexane that crystals from the same batch gave two different sets of cell parameters. It was, however, not possible to differentiate one crystal form from the other based on crystal morphology (prism). Crystals of the same compound obtained from ethanol gave only one of the dimorphs, designated ${ }^{~} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}$ - $b$. The other crystal modification found upon crystallization from cyclohexane (also the only dimorph observed on crystallization from the melt) is designated ${ }^{~} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$. The absolute configurations of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ and its solid-state photoproduct, ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$, have been determined by X-ray anomalousdispersion techniques. To ensure that the absolute configuration of the product can be correlated with that of the starting material, a large single crystal of ${ }^{i} \mathrm{Pr} / \mathrm{Pr}-a$ was grown. A small cut fragment of this crystal was used for data collection and structure determination of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$. Photolysis of the remaining large crystal resulted in ${ }^{1} \mathrm{Pr} / / \mathrm{Pr}-a p$.

The general procedures and parameters of data collection are summarized in Table 1. Intensities were measured at 295 K with a CAD-4F diffractometer, $\omega-2 \theta$ scan (extended $25 \%$ on each side for background measurement), horizontal aperture ( 2.0 $+\tan \theta) \mathrm{mm}$, vertical aperture 4 mm ; three standard reflections measured periodically (no significant intensity variation). Mo $K \alpha$ (graphite monochromator) or $\mathrm{Cu} K \alpha$ (nickel-filtered) radiations were used (Table 1). Two sets of data were collected for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a(h k l$ and $\bar{h} k \bar{l})$ and for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p(h k l, k \geq$ $h$ and $h k l, h \geq k$ ); the two sets of reflections in each case are expected to have slightly different intensities in the presence of anomalous-dispersion effects. Absorption errors are negligible and no corrections were applied. Reflections with $I \geq 3 \sigma(I)$ were considered observed, where $\sigma^{2}(I)=S+4\left(B_{1}+B_{2}\right)+$ $(0.04 S)^{2}$, with $S=$ scan, $B_{1}$ and $B_{2}$ background counts. All three structures were determined by direct methods with the use of MULTAN80,* using the $h k \bar{l}$ data for ${ }^{i} \operatorname{Pr} /{ }^{\prime} \operatorname{Pr}-a$, and $h k l, k \geq h$ data for ${ }^{i} \mathrm{Pr} / / \mathrm{Pr}-a p$. Refinement was by full-matrix leastsquares methods on $F$, minimizing $\sum w\left(\left|F_{o}\right|-\right.$ $\left.k\left|F_{c}\right|\right)^{2}$, with $w=1 / \sigma^{2}(F)$ giving uniform values of $\sum w \Delta F^{2}$. High apparent thermal motion of the terminal methyl C atoms in ${ }^{~} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ indicated some disorder which was resolved after the two sets of data were combined. The disorder was treated by distributing each of the four methyl C atoms involved

[^1]Table 1. Data-collection and refinement parameters for dibenzobarrelenes and dibenzosemibullvalene

|  | ${ }^{\prime} \mathrm{Pr} / \mathbf{} / \mathbf{P r}-a$ | ${ }^{\text {'Pr/'Pr}}$ - $b$ |  |
| :---: | :---: | :---: | :---: |
| Solvent | Cyclohexane | Ethanol | Ethanol |
| Dimensions (cut fragments) (mm) | $0.3 \times 0.25 \times 0.2$ | $0.35 \times 0.3 \times 0.3$ | $0.35 \times 0.35 \times 0.3$ |
| Radiation | $\mathrm{Cu} K \alpha_{1}$ | Mo $K \alpha_{1}$ | $\mathrm{Cu} K \alpha_{1}$ |
| Reflections for cell |  |  |  |
| No. | 25 | 25 | 25 |
| $\theta$ range ( ${ }^{\circ}$ ) | 25-41 | 10-12 | 22-42 |
| Intensity measurements |  |  |  |
| $\theta_{\max }\left({ }^{\circ}\right.$ ) | 75.0 | 25.0 | 75.0 |
| $\omega$ scan, $(a+b \tan \theta), a\left({ }^{\circ}\right)$ | 0.55 | 0.75 | 0.55 |
| $\omega \operatorname{scan},(a+b \tan \theta), b\left(^{\circ}\right)$ | $0 \cdot 14$ | 0.35 | $0 \cdot 14$ |
| Scan speed ( ${ }^{\circ} \mathrm{min}^{-1}$ ) | 1.26-10.06 | 1-18-10.06 | 1.01-10.06 |
| $h$ | $0 \rightarrow 10$ | $0 \rightarrow 11$ | $0 \rightarrow 12$ |
| $k$ | $0 \rightarrow 14$ | $0 \rightarrow 20$ | $0 \rightarrow 12$ |
| 1 | $-27 \rightarrow 0$ | $0 \rightarrow 29$ | $0 \rightarrow 48$ |
| Total unique reflections (both sets) | 2501 (4688) | 3655 | 2483 (4627) |
| Reflections with $I \geq 3 \sigma(I)$ | 1691 (3101) | 1299 | 1553 (2879) |
| \% (for a unique set) | 67.6 | $35 \cdot 5$ | 62.5 |
| Structure refinements |  |  |  |
| No. of parameters refined | 250 | 254 | 350 |
| Data/parameter ratio | 6.8 | $5 \cdot 1$ | 7.1 |
| $\Delta / \sigma$ mean | 0.007 | 0.001 | 0.006 |
| maximum | 0.095 | 0.004 | 0.071 |
| $\Delta \rho\left(\mathrm{e} \AA^{-3}\right)$ | $-0.70 \rightarrow 0.51$ | $-0.15 \rightarrow 0.23$ | $-0.32 \rightarrow 0.36$ |
| $R[I \geq 3 \sigma(I)]$ | 0.069 | 0.044 | 0.036 |
| $w R$ | 0.082 | 0.046 | 0.038 |
| $S$ (goodness of fit) | 3.19 | 1.51 | 1.39 |
| $R$ (all data) | 0.102 | 0.180 | 0.077 |
| Extinction, $g$ | $5.3(6) \times 10^{4}$ | $12(2) \times 10^{4}$ | $2.6(2) \times 10^{4}$ |

over two sites and adjusting the split atom occupancies until the isotropic temperature factors of an atom and its split counterpart were approximately the same. The final occupancies that gave the best model are given along with the atomic coordinates. All non- H atoms were allowed to refine anisotropically except the disordered C atoms in ${ }^{i} \mathrm{Pr} /{ }^{\prime} \operatorname{Pr}-a$. H atoms of the two dibenzobarrelenes were placed in calculated positions while the H atoms of the product were refined isotropically after the two sets of data were combined.

## Absolute configurations

Before anomalous-dispersion effects were taken into account, the Bijvoet pairs for each chiral structure were included separately in the data sets, taking care not to have duplications for reflections $h=0$ for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ and $h=k$ for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$. From the final coordinates obtained from the unique sets of data refinement, the coordinates of the corresponding enantiomorphous molecules for the two compounds were generated (for ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}$ - $a p$ that meant a change of space group from $P 4_{1} 2_{1} 2$ to $P 4_{3} 2_{1}$ 2) and both enantiomorph configurations were refined using the respective combined sets of data for each compound. The final weighted $R$ factors obtained from the refinements are $w R$ [structure (1)] $=0.089886$ and $w R$ [structure (2)] $=0.089815$ for ${ }^{i} \operatorname{Pr} /{ }^{\prime} \mathrm{Pr}-a$, and $w R$ $\left(P 4_{1} 2_{2} 2\right)=0.038525$ and $w R\left(P 4_{3} 2_{1} 2\right)=0.038283$ for ${ }^{i} \operatorname{Pr} /{ }^{\prime} \operatorname{Pr}-a p$. The quoted $w R$ 's for ${ }^{i} \operatorname{Pr} /{ }^{\prime} \operatorname{Pr}-a$ are before the disorder was treated. Hamilton's (1965) $R$-factor

Table 2. Comparison of observed and calculated values of $\Delta$ for the correct absolute configuration of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-\mathrm{a}$

| $h$ | $k$ | $l$ | $\Delta_{l}$ | $\Delta_{\text {av }}$ | $\Delta_{c}$ | $h$ | $k$ | $l$ | $\Delta_{o}$ | $\Delta_{\text {av }}$ | $\Delta_{c}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 2 | 1 | -20 | 0.087 | 0.102 | 0.040 | 3 | 5 | -17 | -0.366 | 0.064 | 0.035 |
| 2 | 8 | -2 | -0.120 | 0.006 | 0.032 | 2 | 1 | -13 | -0.117 | 0.009 | 0.030 |
| 3 | 5 | -10 | 0.015 | 0.024 | 0.028 | 3 | 2 | -23 | 0.375 | 0.124 | 0.026 |
| 3 | 3 | -3 | -0.049 | -0.021 | 0.026 | 6 | 4 | -17 | -0.173 | -0.096 | 0.025 |
| 1 | 4 | -12 | 0.213 | 0.121 | 0.024 | 4 | 7 | -8 | 0.016 | -0.009 | 0.024 |
| 1 | 3 | -9 | 0.121 | 0.112 | 0.023 | 3 | 7 | -5 | -0.129 | -0.092 | 0.022 |
| 2 | 9 | -8 | 0.020 | 0.061 | 0.022 | 1 | 7 | -20 | 0.031 | 0.015 | 0.022 |
| 5 | 5 | -8 | 0.041 | 0.059 | 0.022 | 2 | 9 | -13 | -0.035 | 0.008 | -0.021 |
| 4 | 4 | -6 | -0.104 | -0.072 | -0.022 | 5 | 5 | -17 | -0.005 | -0.012 | -0.022 |
| 2 | 6 | -9 | -0.176 | -0.102 | -0.023 | 3 | 7 | -3 | -0.103 | -0.083 | -0.024 |
| 2 | 5 | -18 | -0.042 | 0.024 | -0.026 | 4 | 8 | -15 | -0.345 | -0.136 | -0.027 |
| 3 | 1 | -9 | 0.056 | -0.062 | -0.027 | 4 | 6 | -4 | -0.367 | -0.141 | -0.027 |
| 4 | 4 | -19 | 0.119 | 0.094 | -0.030 | 1 | 11 | -10 | 0.221 | 0.078 | -0.028 |
| 5 | 3 | -11 | 0.530 | 0.159 | -0.034 | 3 | 5 | -6 | 0.014 | 0.029 | -0.037 |
| 1 | 4 | -1 | -0.227 | -0.196 | -0.037 | 6 | 3 | -5 | -0.076 | -0.056 | -0.049 |

Table 3. Comparison of observed and calculated values of $\Delta$ of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}$-ap for the space group $\mathrm{P}_{3} 2_{1} 2$ (the correct configuration)

| $h$ | $k$ | $l$ | $\boldsymbol{\Delta}_{o}$ | $\Delta_{\mathrm{av}}$ | $\boldsymbol{\Delta}_{c}$ | $h$ | $k$ | $l$ | $\Delta_{o}$ | $\boldsymbol{\Delta}_{\mathrm{av}}$ | $\boldsymbol{\Delta}_{c}$ |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 6 | 3 | 2 | 0.239 | 0.100 | -0.033 | 7 | 5 | 13 | -0.074 | -0.161 | -0.026 |
| 5 | 1 | 10 | 0.273 | 0.009 | -0.021 | 4 | 1 | 5 | -0.174 | -0.150 | -0.023 |
| 8 | 3 | 3 | 0.042 | -0.169 | -0.021 | 10 | 2 | 8 | -0.039 | -0.061 | -0.018 |
| 5 | 4 | 2 | 0.059 | -0.043 | 0.017 | 8 | 3 | 4 | 0.068 | -0.098 | 0.019 |
| 8 | 4 | 1 | 0.059 | 0.012 | 0.018 | 9 | 5 | 9 | -0.014 | -0.117 | 0.018 |
| 5 | 4 | 9 | 0.553 | 0.184 | 0.019 | 10 | 1 | 6 | 0.140 | 0.069 | 0.020 |
| 11 | 2 | 3 | 0.003 | 0.156 | 0.018 | 6 | 2 | 5 | 0.491 | 0.019 | 0.021 |
| 10 | 5 | 10 | -0.183 | 0.029 | 0.025 | 5 | 2 | 11 | 0.084 | 0.074 | 0.026 |
| 6 | 4 | 4 | 0.077 | 0.052 | 0.026 | 5 | 3 | 16 | -0.095 | -0.007 | 0.028 |
| 3 | 2 | 14 | 0.023 | 0.100 | 0.027 | 4 | 2 | 4 | 0.205 | 0.050 | 0.031 |

ratio test on these values shows that the molecular models in structure (2) and in space group $P 4_{3} 2_{1} 2$ fit the respective observed data better than their opposite models at confidence levels of about 95 and $99 \%$, respectively. However, this test may not be completely reliable (Rogers, 1981), especially given the small values for $\Delta f^{\prime \prime}(0.009$ for $\mathrm{C}, 0.032$ for O ), and further tests for the absolute configurations employed the Bijvoet difference method (Bijvoet, Peerdeman \& Van Bommel, 1951; Hope \& de la Camp, 1972; Pennington, Chakraborty, Paul \& Curtin, 1988). The differences between the $F$ values of 30 Friedel pairs with the largest $\Delta_{c}$ 's were calculated for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$, while 20 pairs were calculated for ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a p$. Tables 2 and 3 compare the observed and calculated values of $\Delta=\left(\left|F_{h k \lambda}^{2}\right\rangle-\left|F_{h k}^{2}\right|\right) /\left[0 \cdot 5\left(\left|F_{h k}^{2}\right| \mid\right.\right.$ $\left.\left.+\left|F_{h k I}^{2}\right|\right)\right]$ for $h \neq 0$, and $\Delta=\left(\left|F_{h k \mid}^{2}\right|-\left|F_{k h l \mid}^{2}\right|\right) /$ $\left[0 \cdot 5\left(\left|F_{h k \mid}^{2}\right|+\left|F_{k h l}^{2}\right|\right)\right]$ for $h \neq k$ for the correct absolute configurations of ${ }^{i} \mathrm{Pr} / /^{\prime} \mathrm{Pr}-a$ and ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$, respectively. It is observed from Table 2 that the signs of $\Delta_{o}$ and $\Delta_{c}$ are the same for 19 (out of 30 ) reflections, and 14 (out of 20) from Table 3. In addition the intensities of the Friedel pairs were remeasured successively at the same scan rate and time. Each Friedel pair was measured six times and the average intensity of each reflection calculated. $\Delta_{\mathrm{av}}$ in the tables corresponds to the Bijvoet difference of the remeasured and averaged intensities. It is apparent from the tables that the signs for $\Delta_{o}$ and the corresponding $\Delta_{\mathrm{av}}$ agree except in seven instances for
${ }^{i} \mathrm{Pr} / / \mathrm{Pr}-a$ and four for ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a p$. The signs for $\Delta_{\mathrm{av}}$ and $\Delta_{c}$ are the same for 20 (out of 30) reflections for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ and 14 (out of 20 ) for ${ }^{~} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$, although not necessarily involving the same reflections as those whose Bijvoet difference signs agreed for $\Delta_{o}$ and $\Delta_{c}$. The lack of complete agreement in the signs of the corresponding $\Delta$ 's for all the reflections in the tables is not surprising since $\Delta f^{\prime \prime}$ values are small. In addition the $\Delta_{o}$, and to some extent the $\Delta_{\mathrm{av}}$ values, are generally larger than $\Delta_{c}$; this is not unexpected, since the errors in measurement of $\Delta_{o}$ are much larger than the small anomalous-dispersion differences in $\Delta_{c}$. All three tests for each structure (Hamilton's test, Bijvoet's test and remeasured Bijvoet data) consistently gave the same results; hence, although the determinations are not completely conclusive, the indications are that the correct absolute configurations have been assigned. Scattering factors were from International Tables for X-ray Crystallography (1974). Details of the refinements are in Table 1.

## Discussion

Final positional parameters are in Table 4; selected bond lengths and angles involving non- H atoms are in Table 5.* Fig. 2 shows the stereo diagrams of the three molecules with atomic numbering. The geometrical parameters involving the disordered atoms are poorly determined and a relatively large dispersion of individual bond lengths and angles is observed. There are relatively large thermal vibrations in the terminal C atoms of the ester groups of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-b$, indicative of some disorder; however, no attempts were made to resolve the disorder as no new structural information related to the photochemistry would be provided by splitting the atoms with high anisotropic thermal parameters. Also, the anisotropies of the thermal parameters of the atoms involved in the apparent disorder of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-b$ are relatively smaller than those observed in ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ before its disorder was resolved.

Some of the aromatic rings in all three structures show small, but not structurally significant deviations from planarity, $\chi^{2}$ values being $3 \cdot 2,28 \cdot 2$ for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a, 6 \cdot 3,25 \cdot 2$ for ${ }^{3} \mathrm{Pr} /{ }^{2} \mathrm{Pr}-b$, and $1 \cdot 15,19 \cdot 84$ for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$. The maximum displacements of C atoms from the respective least-squares mean planes of the most non-planar rings are 0.016 (5) $\AA$ for ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$, and 0.009 (3) $\AA$ each for ${ }^{i} \mathrm{Pr} /{ }^{\circ} \mathrm{Pr}-b$ and ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a p$. The dibenzobarrelene ring skeletons in the dimorphs are

* Lists of anisotropic thermal parameters, bond lengths, bond angles and torsion angles, H -atom parameters, and structure factors, and packing diagrams have been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 52682 ( 90 pp.). Copies may be obtained through The Technical Editor, International Union of Crystallography, 5 Abbey Square, Chester CHI 2HU, England.

Table 4. Final positional (fractional $\times 10^{4}$ ) and equivalent isotropic thermal parameters ( $U \times 10^{3} \AA^{2}$ ), with estimated standard deviation in parantheses

| $U_{\text {cq }}={ }_{3}^{1} \sum_{i} \sum_{j} U_{i j} a_{i}{ }^{*} a_{j}{ }^{*} \mathbf{a}_{i} \cdot \mathbf{a}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $x$ | $y$ | $z$ | $U_{\infty}$ |
| ${ }^{\text {Pr }} / \mathbf{/} \mathrm{Pr}-a$ |  |  |  |  |
| C1 | 7231 (5) | 4835 (4) | 838 (2) | 60 |
| C2 | 7761 (6) | 4136 (5) | 362 (2) | 65 |
| C3 | 6715 (6) | 3617 (4) | -13 (2) | 65 |
| C4 | 5072 (6) | 3721 (4) | 73 (2) | 54 |
| C4a | 4517 (5) | 4418 (3) | 545 (2) | 46 |
| C5 | 1566 (6) | 6563 (5) | 325 (2) | 73 |
| C6 | 1611 (8) | 7782 (5) | 344 (3) | 79 |
| C7 | 2680 (8) | 8328 (5) | 705 (3) | 84 |
| C8 | 3761 (7) | 7696 (4) | 1072 (2) | 69 |
| C8a | 3717 (5) | 6530 (4) | 1057 (2) | 48 |
| C9 | 4793 (5) | 5713 (4) | 1413 (2) | 46 |
| C9a | 5631 (5) | 4987 (4) | 925 (2) | 49 |
| C10 | 2810 (5) | 4667 (4) | 719 (2) | 45 |
| Cl0a | 2624 (5) | 5975 (4) | 679 (2) | 51 |
| $\mathrm{Cl1}$ | 3682 (5) | 4904 (4) | 1756 (2) | 47 |
| C 12 | 2627 (4) | 4376 (4) | 1399 (2) | 45 |
| Cl 3 | 3934 (5) | 4733 (4) | 2424 (2) | 51 |
| C14 | 4162 (9) | 5661 (5) | 3392 (2) | 90 |
| C 15 (0.7) | 2564 (14) | 5351 (11) | 3727 (5) | 122 |
| $\mathrm{Cl5}^{\prime}(0.3)$ | 3288 (33) | 6610 (24) | 3696 (12) | 112 |
| C 16 (0.6) | 4545 (20) | 6826 (14) | 3556 (7) | 128 |
| $\mathrm{Cl}^{\prime} 6^{(0.4)}$ | 5708 (26) | 6440 (20) | 3464 (10) | 126 |
| C 17 | 1380 (5) | 3555 (4) | 1590 (2) | 52 |
| C18 | -129 (10) | 2759 (9) | 2427 (3) | 118 |
| C19 (0.6) | -1625 (17) | 3288 (13) | 2461 (6) | 103 |
| C19' (0.4) | -1418 (28) | 3774 (21) | 2706 (11) | 126 |
| C20 (0.7) | 461 (16) | 2362 (14) | 3041 (7) | 137 |
| C20' (0.3) | 331 (41) | 1910 (32) | 2756 (20) | 138 |
| Ol | 3706 (5) | 5671 (3) | 2737 (1) | 84 |
| O 2 | 4388 (6) | 3860 (3) | 2642 (1) | 91 |
| 03 | 1088 (5) | 3593 (4) | 2172 (2) | 102 |
| 04 | 698 (5) | 2945 (4) | 1241 (2) | 88 |
| ${ }^{\prime} \mathrm{Pr} /$ / $\mathrm{Pr}-b$ |  |  |  |  |
| Cl | 12780 (5) | 2136 (3) | 6502 (2) | 52 |
| C2 | 13182 (6) | 2497 (4) | 6973 (3) | 63 |
| C3 | 12266 (7) | 2967 (4) | 7244 (2) | 63 |
| C4 | 10929 (6) | 3082 (3) | 7063 (2) | 49 |
| C4a | 10532 (5) | 2712 (3) | 6599 (2) | 40 |
| C5 | 8854 (5) | 3704 (3) | 5538 (2) | 52 |
| C6 | 9256 (7) | 3898 (3) | 5024 (3) | 67 |
| C7 | 10176 (7) | 3439 (4) | 4750 (3) | 73 |
| C8 | 10701 (6) | 2766 (3) | 4984 (2) | 57 |
| C8a | 10310 (5) | 2567 (3) | 5492 (2) | 43 |
| C9 | 10822 (5) | 1883 (3) | 5820 (2) | 44 |
| C9a | 11449 (5) | 2240 (3) | 6319 (2) | 41 |
| C10 | 9120 (5) | 2753 (3) | 6332 (2) | 40 |
| C10a | 9391 (5) | 3037 (3) | 5769 (2) | 41 |
| $\mathrm{Cl1}$ | 9527 (5) | 1445 (3) | 6011 (2) | 43 |
| C12 | 8662 (5) | 1897 (3) | 6289 (2) | 38 |
| C 13 | 9271 (7) | 607 (3) | 5889 (2) | 52 |
| C14 | 10366 (7) | -643 (3) | 5798 (3) | 73 |
| C15 | 9840 (8) | - 1044 (3) | 6284 (3) | 98 |
| Cl 16 | 11768 (9) | -891 (4) | 5636 (4) | 136 |
| Cl 17 | 7332 (6) | 1670 (3) | 6537 (2) | 41 |
| C 18 | 6168 (7) | 748 (4) | 7083 (3) | 84 |
| C19 | 5515 (9) | 171 (6) | 6736 (4) | 141 |
| C20 | 6571 (11) | 426 (6) | 7608 (4) | 172 |
| O 1 | 10455 (4) | 206 (2) | 5895 (1) | 62 |
| 02 | 8171 (4) | 332 (2) | 5792 (2) | 76 |
| 03 | 7438 (4) | 1037 (2) | 6837 (2) | 65 |
| 04 | 6317 (4) | 2056 (2) | 6493 (2) | 66 |
| ${ }^{\text {'Pry }} / \mathrm{Pr}-a p$ |  |  |  |  |
| C1 | 6054 (3) | - 1627 (3) | 6188 (1) | 58 |
| C2 | 6968 (3) | - 2628 (3) | 6181 (1) | 68 |
| C3 | 7376 (3) | - 3155 (3) | 5871 (1) | 67 |
| C4 | 6883 (3) | - 2705 (3) | 5560 (1) | 54 |
| C4a | 5959 (2) | -1701 (2) | 5566 (1) | 46 |
| C5 | 7018 (3) | 2227 (3) | 5381 (1) | 49 |
| C6 | 7522 (3) | 2987 (3) | 5648 (1) | 60 |
| C7 | 7063 (3) | 2832 (3) | 5979 (1) | 64 |
| C8 | 6121 (3) | 1910 (3) | 6059 (1) | 56 |
| C8a | 5610 (2) | 1160 (2) | 5793 (1) | 42 |
| C9 | 4665 (2) | 8 (3) | 5814 (1) | 44 |
| C9a | 5545 (2) | -1165 (2) | 5881 (1) | 46 |
| C10 | 5251 (2) | - 1066 (2) | 5276 (1) | 44 |
| C10a | 6054 (2) | 1309 (2) | 5455 (1) | 40 |
| C11 | 4219 (2) | -181 (2) | 5433 (1) | 41 |

Table 4 (cont.)

|  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: |
| C12 | 5320 (2) | 429 (2) | 5214 (1) |
| C13 | 2837 (2) | -156(2) | 5317 (1) |
| C14 | 592 (2) | -179 (3) | 5506 (1) |
| C15 | 151 (4) | - 1505 (4) | 5380 (1) |
| C16 | -74 (3) | 207 (4) | 5837 (1) |
| C17 | - 5090 (2) | 838 (2) | 4845 (1) |
| Cl 8 | 4608 (3) | 2683 (3) | 4485 (1) |
| C19 | 3160 (4) | 2749 (5) | 4444 (1) |
| C20 | 5213 (9) | 4045 (6) | 4492 (2) |
| O1 | 2005 (1) | -218(2) | 5585 (0.4) |
| O 2 | 2505 (2) | -91 (2) | 5019 (0.4) |
| O3 | 4880 (2) | 2117 (2) | 4824 (0.4) |
| O4 | 5113 (2) | 101 (2) | 4600 (0.4) |

Table 5. Selected bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$, with standard deviations in parentheses

|  | ${ }^{\prime} \mathrm{Pr} /$ / $\mathrm{Pr}-\mathrm{a}$ | ${ }^{\prime} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-b$ | ${ }^{\text {' }} \mathrm{Pr} /$ / Pr -ap |
| :---: | :---: | :---: | :---: |
| C-C (aromatic) | 1.34-1.43 (1) | 1.372-1.394 (7) | 1.374-1.399 (4) |
| C9-C11 | 1.521 (6) | 1.543 (7) | 1.550 (3) |
| $\mathrm{Cl} 0-\mathrm{Cl1}$ | - | - | $1 \cdot 513$ (3) |
| $\mathrm{Cl} 0-\mathrm{ClOa}$ | 1.541 (6) | 1.517 (6) | - |
| $\mathrm{Cl} 0-\mathrm{Cl} 2$ | 1.528 (6) | 1.533 (6) | 1.543 (3) |
| $\mathrm{Cl0a}-\mathrm{Cl2}$ | - | - | 1.494 (3) |
| $\mathrm{Cl} 1-\mathrm{Cl} 2$ | 1.328 (5) | 1.339 (6) | 1.537 (3) |
| Cl1-C13 | 1.485 (5) | 1.486 (7) | 1.479 (3) |
| C12-C17 | 1.477 (6) | 1.487 (6) | 1.503 (3) |
| C13-O1 | $1 \cdot 307$ (5) | $1 \cdot 342$ (6) | $1 \cdot 340$ (3) |
| $\mathrm{C13-O} 2$ | $1 \cdot 189$ (5) | 1-195 (6) | 1.200 (3) |
| C17-O3 | $1 \cdot 294$ (5) | 1-322 (5) | 1-323 (3) |
| C17-O4 | $1 \cdot 189$ (5) | 1-194 (5) | 1.207 (3) |
| $\mathrm{C}-\mathrm{C}-\mathrm{C}$ (aromatic) | 118.2-121-8 (5) | 118.2-121.7 (6) | 118.3-121.5 (3) |
| C9-C8a-C10a | 113.3 (4) | 112.7 (5) | 109.8 (2) |
| C9-C9a-C4a | 111.6 (3) | 112.9 (4) | 109.7 (2) |
| $\mathrm{Cl0}-\mathrm{C} 4 \mathrm{a}-\mathrm{C} 9 \mathrm{a}$ | 112.7 (3) | 112.4 (4) | 110.0 (2) |
| C10-C10a-C8a | 111.4 (4) | 113.2 (5) | - |
| C12-C10a-C8a | - | - | 111.0 (2) |
| C9-C11-C12 | 114.0 (3) | 113.4 (4) | 105.1 (2) |
| $\mathrm{Cl} 0-\mathrm{Cl} 2-\mathrm{Cll}$ | $113 \cdot 5$ (3) | 113.8 (4) | 58.8 (2) |

similar to each other and to that of dibenzobarrelene itself (Trotter \& Wireko, 1990) and those of other 11,12-diester derivatives (Garcia-Garibay et al., 1990). There are systematic angular deformations from $120^{\circ}$ (Allen, 1981a) at the benzene-cyclohexene ring junctions (mean angle $=112 \cdot 5^{\circ}$ ) which are characteristic of these structures; there are relatively greater angular deformations at the benzenecyclopentane ring junctions of the dibenzosemibullvalene photoproduct (mean angle $=110 \cdot 1^{\circ}$ ), suggesting that such angular distortions are a function of ring size. Bond lengths and angles in the aromatic rings of all three compounds are close to expected values, with mean $\mathrm{C}-\mathrm{C}_{\text {aromatic }}=1.384,1.385$, $1 \cdot 384 \AA$, and $\mathrm{C}-\mathrm{C}-\mathrm{C}_{\text {aromatic }}=120^{\circ}$ each for ${ }^{i} \mathrm{Pr} /{ }^{\mathrm{i}} \mathrm{Pr}$ $a,{ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-b$, and ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$, respectively. The lengths of the bridging double bonds $(\mathrm{Cll}=\mathrm{Cl} 2)$ are not significantly different for ${ }^{i} \operatorname{Pr} / 2 \operatorname{Pr}-a[1-328(5) \AA]$ and ${ }^{i} \operatorname{Pr} /{ }^{i} \operatorname{Pr}-b[1.339$ (6) $\AA]$, and are in agreement with the equivalent bridge-bond length of $1 \cdot 334$ (5) $\AA$ in the methyl isopropyl diester derivative (Garcia-Garibay et al., 1990), but significantly longer than that in dibenzobarrelene itself [1.316(4) $\AA$ ] (Trotter \& Wireko, 1990).

The isopropyl ester groups in the starting materials are geometrically inequivalent, especially in the
degree of conjugation of the carbonyl groups to the vinyl double bond $(\mathrm{C} 11=\mathrm{C} 12)$. The dihedral angles $\mathrm{C} 2-\mathrm{C} 11-\mathrm{Cl} 3-\mathrm{O} 2\left(\varphi_{1}\right)$ and $\mathrm{Cl1}-\mathrm{Cl} 2-$ C17-O4 ( $\varphi_{2}$ ) are $64 \cdot 1(7)$ and $-164 \cdot 3(5)^{\circ}$, respectively, for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ and $36 \cdot 1$ (9) and $-134 \cdot 1$ (6) ${ }^{\circ}$ for ${ }^{i} \operatorname{Pr} /{ }^{\prime} \operatorname{Pr}-b$. Thus, in both structures, one $\mathrm{C}=\mathrm{C}-\mathrm{C}=\mathrm{O}$ system is syn and the other anti, and the two ester groups are only partially conjugated to the central double bond but to different extents; the carbonyl group at C 12 of ${ }^{i} \mathrm{Pr} / \mathrm{Pr}-a\left(\cos ^{2} \varphi_{2}=0.93\right)$ is more conjugated to the central vinyl bond $\mathrm{Cll}=\mathrm{C} 12$ than the ester carbonyl group at $\mathrm{Cl1}\left(\cos ^{2} \varphi_{1}=0 \cdot 19\right)$.


Fig. 2. Stereoviews of the molecular structures ( $50 \%$ thermal probability ellipsoids for the C and O atoms, arbitrary circles for the H atoms). (a) ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}$ - $a$ (disordered C atom with lower occupancies drawn with empty ellipsoids; H atoms omitted for
 the determined absolute configurations for the crystals studied; crystals of ${ }^{\prime} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-b$ are racemic, and the enantiomorph shown in $(b)$ is numbered to correspond to that shown previously for racemic $\mathrm{Me} /{ }^{\prime} \operatorname{Pr}$ [(Garcia-Garibay et al., 1990, Fig. 2(a)].

There is an additional strain in the product molecule relative to the starting material as a result of the cyclopentane-cyclopropane ring fusion in the product molecule. Bond angles within the cyclopropane ring are within expected values: $58 \cdot 8-60 \cdot 8^{\circ}$. The torsion angles (using the midpoints of the cyclopropane ring bonds, $M_{i j}$ opposite atom $C_{i j}$, Fig. 3), $\tau_{1}$ $(M 11-\mathrm{Cl1}-\mathrm{Cl} 3-\mathrm{O} 2)$ and $\tau_{2}$ (M12-C12-C17-O4) are 10.3 and $46.9^{\circ}$ for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$, respectively. [Note that the ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$ numbering system used (Figs. 2 and 3) corresponds to that of the dibenzobarrelene, ${ }^{i} \operatorname{Pr} /{ }^{i} \operatorname{Pr}-a$, for comparison purposes, rather than to that of the dibenzopentalene ring system.] Thus, $\mathrm{C} 13=\mathrm{O} 2$ shows a cis-bisection conformation with respect to the cyclopropane ring (Allen, 1980, 1981b; Garcia-Garibay et al., 1990). No systematic bond-length asymmetry is, however, apparent in the cyclopropane ring. On the other hand, the bond lengths $\mathrm{C} 11-\mathrm{C} 13[1.479$ (3) $\AA$ ] and $\mathrm{C} 12-\mathrm{C} 17[1.503$ (3) $\AA$ § seem to suggest some extent of conjugation of $\mathrm{Cl3}=\mathrm{O} 2$ to the cyclopropane ring while $\mathrm{C} 17=\mathrm{O} 4$ shows no such effect.

There are some intermolecular contacts in ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ below the sum of the van der Waals radii of the atoms involved: $\mathrm{O} 2 \cdots \mathrm{H} 8$ ( $2.58 \AA$ ), $\mathrm{H} 3 \cdots{ }^{\circ} \mathrm{H}^{\prime} 6 \mathrm{a}^{\prime}$ (2.30 $\AA$ ), $\quad \mathrm{H} 15 \mathrm{~b}^{\prime} \cdots \mathrm{H} 19 \mathrm{c} \quad(2 \cdot 30 \AA), \quad \mathrm{H} 16 \mathrm{c} \cdots \mathrm{H} 19 \mathrm{c}$ ( $2.31 \AA$ ), $\mathrm{H} 18 \cdots \mathrm{H} 15 \mathrm{c}^{\prime}(2.32 \AA)$, and $\mathrm{H} 18^{\prime} \cdots \mathrm{H} 15 \mathrm{c}^{\prime}$ $(2 \cdot 36 \AA)$, perhaps an artifact of the disorder. There are no such short intermolecular distances in the other structures.

## Structural-photochemical correlations

The commonly accepted mechanism for the di-$\pi$-methane reaction (Zimmerman, 1980) can proceed in the dibenzobarrelene system by four pathways, the first steps of which involve bond formation between vinyl (C11 or C12) and benzo C atoms (Fig. 4). For unsymmetrically substituted derivatives (Fig. 4, $E^{\prime} \neq$ $E$ ) pathways 1 and 2 lead to two isomeric products, each of which has $S, S, S, S$ configuration at the four chiral centres ( $*$ in Fig. 4); pathways 3 and 4 give the enantiomeric $R, R, R, R$ products. A previous study of the solid-state photolysis of the methyl/isopropyl diester $\left(E / E^{\prime}=\mathrm{Me} /{ }^{\prime} \mathrm{Pr}\right.$, Garcia-Garibay et al., 1990) has shown that pathway 2 (and the enantiomeric


Fig. 3. Geometry of the cyclopropane substructure in ${ }^{\prime} \mathrm{Pr} / / \mathrm{Pr}-a p$.



(1)


| Path | Bridging | $E^{\prime} \times E$ | $E^{\prime}=E$ |
| :---: | :---: | :---: | :---: |
| 1 | 11-9a | S.S.S.S. $S$-8C-E ${ }^{\prime}$ |  |
| 2 | 12-10a | S.S.S.S-8c-E $\}$ | S.S.S.S |
| 3 4 | $11-8 \mathrm{a}$ $12-4 \mathrm{a}$ | R,R.R.R-R-8C-E' $R, R, R, B-E-E$ | R.R.R.R |

Fig. 4. The four possible pathways in the di- $\pi$-methane rearrangement of dibenzobarrelenes. Each path involves three steps, e.g. for path 2 , (i) $\mathrm{Cl} 2 \cdots \mathrm{C} 10$ a bond formation [the $\mathrm{C} \cdots \mathrm{C}$ distances in the four pathways are all in the range $2.437-$ 2.442 (6) $\AA$ ], (ii) $\mathrm{C} 10-\mathrm{Cl0a}$ bond breaking, (iii) $\mathrm{C} 10 \cdots \mathrm{Cl} 1$ bond formation. Each photoproduct contains four chiral centres (* in the drawing at upper left), which are $S, S, S, S$ for paths 1 and 2 , and $R, R, R, R$ for paths 3 and 4. Products (2) and (2') are isomers, with either $E^{\prime}$ or $E$ on the central 8 c site (dibenzopentalene numbering system). (The dibenzobarrelene ring system can of course be numbered in four different ways, but all the discussion of the reaction pathways in the text is independent of the numbering system.)
pathway 4 , the crystal structure being centrosymmetric) is predominant in the solid state. This pathway is consistent with intermolecular steric effects, as estimated by qualitative inspection of the crystal packing and by more-quantitative calculation of the van der Waals energy as the ester groups move during the solid-state reaction.

For the symmetrically substituted derivative described in the present paper [Fig. 1; (1), $E^{\prime}=E=$ $\mathrm{CO}_{2}{ }^{i} \mathrm{Pr}$ ), pathways 1 and 2 give rise to identical products $\left[(2)=\left(2^{\prime}\right)\right.$ in Figs. 1 and 4], and pathways 3 and 4 give the enantiomorphic product. The fortuitous crystallization of one dimorph in the chiral space group $P 2_{1} 2_{1} 2_{1}\left({ }^{( } \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a\right)$ and the production of chiral photoproduct on solid-state photolysis of this dimorph permit differentiation between pathways $(1+2)$ and $(3+4)$, by determining the absolute configuration of the molecules of photoproduct. In addition, it may be possible to differentiate between pathways 1 and 2 (or between 3 and 4 ) by determining the absolute configuration of the $P 2_{1} 2_{1} 2_{1}$ crystal and correlating this with the absolute configuration of the photoproduct.

The present study of the $P 2_{1} 2_{1} 2_{1}$ crystal ( $\left.{ }^{( } \operatorname{Pr} / / \operatorname{Pr}-a\right)$ involved growing a large ( 55 mg ) crystal, a small fragment of which was used for the X-ray crystal analysis. The remainder of the large crystal was photolysed and gave laevorotatory photoproduct $\left.{ }^{\circ} \mathrm{Pr} / / \operatorname{Pr}-a p\right),[\alpha]_{D}=-25 \cdot 4^{\circ}\left(\mathrm{CHCl}_{3}\right)$, in quantitative enantiomeric excess. (Presumably multiple crystallizations would give rise to equal amounts of the two chiralities of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$.) The molecular structure of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ can be described by the conformational chirality formalism (Cahn \& Ingold, 1951; Cahn, Ingold \& Prelog, 1966); basically this designates the conformation of an ester group in ${ }^{~} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ as $P$ (for positive) if the $\mathrm{C}=\mathrm{C}-\mathrm{C}=\mathrm{O}$ torsion angle has a positive sign, or as $M$ (for minus) for a negative torsion angle. For the crystal of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-a$ studied, the absolute configuration determined [see Experimental and Fig. 2(a)] is $11 P, 12 M$, i.e. $P$ for the ester group at $\mathrm{Cl1}\left(\mathrm{Cl2}=\mathrm{C} 11-\mathrm{Cl} 3=\mathrm{O} 2=+64^{\circ}\right)$ and $M$ at $\mathrm{C} 12\left(\mathrm{Cl1}=\mathrm{C} 12-\mathrm{C} 17=\mathrm{O} 4=-164^{\circ}\right)$. The corresponding solid-state photoproduct ( ${ }^{( } \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p$ ) crystallizes in space group $P 4_{3} 2,2$, and the absolute configuration of the molecule has been established (see Experimental) as $S, S, S, S$ (Fig. 2c). Thus the solid-state reaction proceeds via pathway 1 (C11-C9a bridging) and/or pathway 2 (C12-C10a bridging), since pathways 3 and 4 would give $R, R, R, R$ photoproduct (Fig. 4). A detailed study of the molecular structure of ${ }^{1} \mathrm{Pr} / \mathrm{Pr}-a$ indicates that carbonyl O 2 is situated above the region of the $\mathrm{C} 4 \mathrm{a}-\mathrm{C} 9 \mathrm{a}$ bond, and ester O 3 above the $\mathrm{Cl} 1-\mathrm{Cl} 2$ bond (Fig. 2a). Pathways 3 (C11-C8a) and 4 (C12-C4a) involve severe intramolecular clashing of the ester groups as they are forced towards each
other in the initial stage of the reaction. In contrast, pathways 1 ( $\mathrm{C} 11-\mathrm{C} 9 \mathrm{a}$ ) and 2 (C12-C10a) involve movement of the ester groups away from one another, thus providing a plausible rationale for the preference for pathways 1 or 2 and the observed $S, S, S, S$ photoproduct.

Another point to consider is whether the pathway leading to the observed photoproduct can be deduced on the basis of odd-electron stabilization (Garcia-Garibay et al., 1990), which predicts that initial vinyl-benzo bridging should occur at the vinyl C atom bearing the ester group which is less conjugated to the central double bond (in this case C11, with $\cos ^{2} \varphi_{1}=0 \cdot 19$, vs $\mathrm{C} 12, \cos ^{2} \varphi_{2}=0.93$ ), since this permits more-extensive electron delocalization in the intermediate biradical. This prediction that Cll should be involved in the initial vinyl-benzo bridging is probably not a very reliable indication, since previous work (Garcia-Garibay et al., 1990) has shown that the electron stabilization effects predict the incorrect regioisomer in the unsymmetrical ester case, and are not the major influence in determining the course of the reaction.
The most useful correlation between reactivity and structure was found previously (Garcia-Garibay et al., 1990) by considering intermolecular steric factors. The reaction pathway involves a large movement of a vinyl C atom and its attached ester group, and the most likely reaction pathway will involve movement of the less-sterically hindered ester group. Data on this point can be obtained by three approaches (Garcia-Garibay et al., 1990). Firstly, qualitative inspection of the packing* in the ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ crystal structure indicates that the isopropyl ester group at C 12 is less sterically hindered than that at $\mathrm{Cl1}$, so that reaction is expected at C12, i.e. pathway 2 (C12-C10a bonding) is the most likely route to the observed $S, S, S, S$ photoproduct.

Secondly, a more-quantitative account of the steric effects is obtained from calculation of the 6-12 Lennard-Jones potential-energy profiles (Hagler, Huller \& Lifson, 1974), which represent the simulated interaction energy as a result of the movements of the vinyl C atoms and their respective ester groups during initial bond formation (Fig. 5). The angle represents rotation around defined vectors (e.g. $\mathrm{C} 10 \cdots \mathrm{C} 11$ ), which moves the appropriate vinyl C atom towards vinyl-benzo bridging: $0^{\circ}$ corresponds to the observed molecular structure, and positive and negative angles correspond to clockwise and anticlockwise rotations, respectively [see Garcia-Garibay et al. (1990) for further details]. The potential energies were calculated with the coordinates of the molecule before the disorder in the region of the isopropyl groups was treated. Clearly the profiles

[^2]suggest that movement of IS19 $\left(\mathrm{CO}_{2}{ }^{i} \mathrm{Pr}\right.$ bonded to C 12 ) corresponds to a lower-energy process than movement of IS15 (bonded to C11), and therefore C 12 is expected to be involved in the initial bond formation. The expanded profile for IS19 (Fig. 5) shows that if C12 is involved in vinyl-benzo bridging, then anticlockwise rotation about the vector $\mathrm{C} 10 \cdots \mathrm{C} 11$ is a less-energetic process than the clockwise rotation. The anticlockwise rotation brings Cl 2 into bond formation with C10a (i.e. pathway 2) \{see Figs. 2(a) and 4; note that Figs. $2(a)$ and 5 of Garcia-Garibay et al. (1990) show a molecule of $\mathrm{Me} / \mathrm{I}^{\mathrm{P}} \mathrm{Pr}$ numbered with the opposite absolute configuration to that determined here for ${ }^{i} \operatorname{Pr} /{ }^{i} \operatorname{Pr}-a$ [the $\mathrm{Me} / \mathrm{Pr}$ crystals are racemic, as are the crystals of ${ }^{i} \mathrm{Pr} / \mathrm{Pr}-b$, and Fig. 2(a) of Garcia-Garibay et al. (1990) and Fig. 2(b) of the present paper depict similar enantiomorphs]\}. The ensuing product from such a bond formation is again consistent with the $S, S, S, S$ absolute configuration of the observed photoproduct.

Thirdly, pathway 2 is the least-motion (topochemically favorable) process, which produces the photoproduct directly in its observed molecular conformation with only minor rotations of the ester groups (Fig. 6). This is indicated quantitatively in Table 6, which shows calculated torsion angles if the ester groups maintain their starting conformations relative to the $\mathrm{Cll}=\mathrm{Cl} 2$ bond, and the differences from the observed torsion angles in the photoproduct. Pathway 2 requires changes of 38 and $-82^{\circ}$ in
the two torsion angles, whereas pathway 1 would require much larger reorientations of nearly $180^{\circ}$. (The reaction is not a topotactic one, and the photoproduct was recrystallized prior to the crystal structure analysis. This third argument is therefore not definitive on its own, but is in accord with the previous steric considerations.) Further, the conformational energy values obtained from $M M P 2$ calculations (Allinger \& Flanagan, 1983) without any minimization show that conformation (2A) in Fig. 6 has a conformational energy higher than that of the observed structure by about $23 \mathrm{kcal} \mathrm{mol}^{-1}$ ( $96 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ), and so is less likely to be formed.
Thus, the correlation of structural and photochemical data has shown that the odd-electron stabilization concept does not seem to explain adequately the solid-state enantioselectivity of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$. The qualitative inspection of the conformations and the lattice environments of the ester groups, complemented by van der Waals energy calculations and comparison of the conformations of reactant and photoproduct indicate that the enantioselective pathway in the solid state is pathway 2 in Fig. 4.

All of the above discussion of the reaction pathway of the photoconversion of ${ }^{i} \mathrm{Pr} / 2 \mathrm{Pr}-a$ to ${ }^{i} \mathrm{Pr} /{ }^{2} \mathrm{Pr}-a p$ is stated in terms of the atomic numbering system of Figs. 2(a) and 4, but is independent of the numbering system. The reaction pathway followed is deduced to be pathway 2 , which involves initial bond formation between the vinyl C atom bonded to the moreconjugated ester group and the neighbouring benzo


C atom which is away from the carbonyl O atom of the less-conjugated ester group, to give the $S, S, S, S$ photoproduct.

Finally, the achiral crystal ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-b$ ( $\mathrm{Pb} c a$ ) gives racemic photoproduct on photolysis. The molecular conformation of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-b$ is very similar to that found in ${ }^{~} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ [Figs. 2(a) and 2(b)], $\varphi_{1}$ and $\varphi_{2}$ torsion angles of 36 and $-134^{\circ}$, respectively, for ${ }^{i} \operatorname{Pr} /{ }^{i} \operatorname{Pr}-b$ (cf. 64 and $-164^{\circ}$ for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ ). Thus all of the considerations discussed above for ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a$ probably apply equally to ${ }^{i} \operatorname{Pr} /{ }^{\prime} \mathrm{Pr}-b$, but since we have not studied the crystal structure of the racemic photoproduct, the process will not be discussed in detail. The reaction pathway for the achiral crystals will again involve initial bond formation between the vinyl C atom [C12 in Fig. 2(b)] bonded to the ester group with $\mathrm{C}=\mathrm{O}$ anti to $\mathrm{C}=\mathrm{C}$, and the neighbouring benzo C atom remote from the carbonyl O atom [ O 2


Crystal conformation
(1)


Fig. 6. Conversion of ${ }^{i} \mathrm{Pr} / /^{\prime} \mathrm{Pr}-a$ (1) to ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-a p[(2 A)$ and (2B)]. Pathway 2 involves $\mathrm{Cl} 2-\mathrm{C} 10$ a bonding, and results directly in a conformation close to that observed for the photoproduct, whereas pathway 1 (Cl1-C9a) would require conformational changes of about $180^{\circ}$ in the ester orientations to produce the observed photoproduct conformation. The shaded circles indicate carbonyl O atoms.

Table 6. Torsion angles $\left({ }^{\circ}\right)$ in the photoreaction of ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}$-a to give ${ }^{i} \mathrm{Pr} /{ }^{i} \mathrm{Pr}-\mathrm{ap}$
${ }^{\prime} \operatorname{Pr} /{ }^{\prime} \mathrm{Pr}-a$
${ }^{i} \mathrm{Pr} /$ 'Pr-ap
Calculated for path 1
Calculated for path 2
Observed
(Calc. - obs.) for path 1
$\mathrm{Cl} 2=\mathrm{Cl} 1-\mathrm{Cl} 3=\mathrm{O} 2$
$\begin{array}{cl}\mathrm{Cl}= & \mathrm{Cl} 2-\mathrm{Cl} 7=\mathrm{O} 4 \\ -164\end{array}$

| -164 | 64 |
| ---: | ---: |
| 64 | -164 |
| 26 | -82 |
| 170 | 146 |
| 38 | -82 |

in Fig. 2(b)] of the syn ester group; for the enantiomer and numbering system shown in Fig. 2(b) this involves $\mathrm{C} 12-\mathrm{C} 4$ a bonding to give finally the $S, S, S, S$ photoproduct (the $R, R, R, R$ isomer being produced simultaneously from the other enantiomer of ${ }^{i} \mathrm{Pr} /{ }^{\prime} \mathrm{Pr}-b$ in the $\mathrm{Pb} c a$ crystal).

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# The Use of Single-Wavelength Anomalous Scattering to Solve the Crystal Structure of a Gramicidin A/Caesium Chloride Complex 

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#### Abstract

Single-wavelength $\mathrm{Cu} K \alpha$ anomalous scattering has been used to determine the structure of a crystalline complex of gramicidin A and caesium chloride. The asymmetric unit in these crystals, with space group $P 2_{1} 2_{1} 2_{1}$ and $a=32 \cdot 118(6), \quad b=52 \cdot 103(12), \quad c=$ $31 \cdot 174$ (7) $\AA$, contains four independent monomers (two dimers) of the pentadecapeptide. This structure falls in an intermediate size range for which direct methods and multiple isomorphous replacement are generally not successful for obtaining phase information. However, using the Bijvoet differences and the partial structure of the caesium atoms which have been incorporated in the crystals, it has been possible to obtain information on this crystal form. Because the caesium atoms dominate the scattering of these crystals, inclusion of the Friedel mate information in the restrained least-squares refinement has been essential. These studies extend the utility of singlewavelength anomalous-scattering phase determination to a macromolecular structure in which the partial structure of the anomalous scatterer is large.


## Introduction

Gramicidin A is a linear pentadecapolypeptide antibiotic which forms dimeric channels in biological

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membranes; these channels are specific for the conductance of monovalent cations (Hladky \& Haydon, 1972; Veatch \& Stryer, 1977). Until recently (Wallace \& Ravikumar, 1988; Langs, 1988), no crystal structure of gramicidin had been solved at the molecular level, because the molecule falls in a difficult size range for crystallographic studies: rather large for direct methods, and because of the difficulty in forming isomorphous derivatives of this flexible molecule, somewhat small for multiple isomorphous replacement phasing.

This paper describes the use of anomalous scattering from caesium atoms at a single wavelength ( $1.54 \AA$ ) far removed from the absorption edge of caesium for phase determination in crystals containing a complex of gramicidin and caesium chloride. This type of approach (Hendrickson, Smith \& Sheriff, 1985), in which the phases are determined from a combination of the Bijvoet differences and the partial structure of the anomalous scatterer in a single crystal, has been used to solve the structures of a number of macromolecules, including crambin (Hendrickson \& Teeter, 1981), myohemerythrin (Smith \& Hendrickson, 1982) and trimeric hemerythrin (Smith, Hendrickson \& Addison, 1983). In each of these cases, the anomalous scatterer was present in the native protein (the sulfur atoms of the cysteine side chains in crambin, and the iron centers in myohemerythrin and trimeric hemerythrin), and had © 1990 International Union of Crystallography


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[^1]:    * Programs used include locally written programs and locally modified versions of MULTAN80 (Main, Fiske, Hull, Lessinger, Germain, Declercq \& Woolfson, 1980); ORFLS and ORFFE (Busing, Martin \& Levy, 1962, 1964), and ORTEPII (Johnson, 1976).

[^2]:    * See deposition footnote re packing diagram.

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